

# What is Econometrics?

# Parameters

- The *parameters* we have studied so far are means or proportions (rates).
- We've also studied differences between means and proportions.

# New Parameters

- But imagine a relationship between two random variables, labelled  $y$  and  $x$ , given by:

$$y = b_0 + b_1 x + e$$

where  $e$  is a random error with a mean of zero.

- And now imagine the population values of  $b_0$  and  $b_1$  are the parameters we are interested in.

# Examples: Response/Explanatory

- $y$   $x$
- life expectancy GDP per capita
- alcohol consumption alcohol price index
- (these vary in a cross-section)
- average temperature CO<sub>2</sub> ppm
- exchange rate previous day's value
- (these vary over time)

# Estimation

- We can estimate the two parameters with point estimates or form confidence intervals.
- The usual way to do this is called regression, or ordinary least squares regression (OLS)

# Least Squares

- Visualize the scatter plot of  $y$  versus  $x$ .
- Imagine drawing a straight line through the points.
- OLS formulas, in software, minimize the sum of squared departures from the line so the line fits the data as closely as possible.

# Applet

- Experiment with the applet

*correlationregression*

- You can see how the sum of squared residuals rises and falls as you adjust the line.
- Software performs this task for us with actual data.

- We also could fit curves, for example if we think  $y$  is related to the square of  $x$  or some other functional form.
- The results include estimates of  $b_0$  and  $b_1$ , along with *standard errors*. Thus we can form confidence intervals or test hypotheses.



# Hypothesis Tests

- *e.g.* Ho: The effect of alcohol prices on consumption is zero.
- *e.g.* Ho: \$10000 of GDP per capita leads to 3 extra years of life expectancy.
- We can test these hypotheses with *t*-tests.

# Fit and Prediction

- We also can report on the overall fit of the regression line, using a statistic called R-squared ( $R^2$ ). It gives the percentage of the variation in  $y$  explained by  $x$ .
- And, if the line fits well, we can use it to predict or forecast values of  $y$ .

# Applet

- We can use the applet  
*twovar*  
to see how well a regression fits.
- Select a data set, then look at the scatterplot (showing the least-squares line).
- Finally, look at the correlation and regression tab for the corresponding statistics.

# Multiple Regression

- We can control for other influences on  $y$ , by using multiple regression:

$$y = b_0 + b_1x_1 + b_2x_2$$

*e.g. Do wages ( $y$ ) depend on education ( $x_1$ ) or seniority ( $x_2$ ) or both?*

# Warnings

- Remember to always plot your data (with a scatter plot or time series plot, or both). This helps you check for errors or outliers.
- Also remember that correlation (or a fitted regression) does not imply causation. We need theory or experiments to interpret the results.

# Running a Regression

- In econometrics we usually use free software (like *gretl*) or widely-used professional software (like *stata*).
- But you can try your own examples in *excel*, with 2 columns of data and the *data* tab, then the *data analysis* pack, then the *regression* choice.