## ECON 815

## Macroeconomic Theory

Winter Term 2012/13
Assignment 4-ANSWER KEY

## 1 The Empirics of Growth

(1b) The OLS estimates of the parameters are as follows (s.e. in brackets):

| $\widehat{\beta}_{0}$ | $\widehat{\beta}_{1}$ | $\widehat{\sigma}^{2}$ | $R^{2}$ |
| :--- | :--- | :--- | :--- |
| -0.266 | 0.0943 | 0.194 | 0.0363 |
| $(0.380)$ | $(0.0496)$ |  |  |

Table 1: OLS Estimates - Part 1
(1c) We reject the null at the $6 \%$ level. The $95 \%$ confidence interval for $\beta_{1}$ is $[-0.0042,0.1928]$. The speed of convergence is: $\lambda=-\frac{\log \left(1+\widehat{\beta}_{1}\right)}{T}=-\frac{\log (1+0.0943)}{25}=-0.00360$.
(2b-c) The OLS estimates of the parameters are as follows (s.e. in brackets):

| Specification | $\widehat{\beta}_{0}$ | $\widehat{\beta}_{1}$ | $\widehat{\beta}_{2}$ | $\widehat{\sigma}^{2}$ | $R^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $($ OLS $)$ | 5.429 | 1.424 | -1.989 | 0.474 | 0.6009 |
|  | $(1.583)$ | $(0.143)$ | $(0.563)$ |  |  |
| $(R L S)$ | 6.872 | 1.487 |  | 0.474 | 0.5974 |
|  | $(0.120)$ | $(0.124)$ |  |  |  |

Table 2: OLS Estimates - Part 2
(2b) We do not reject the null, because the $F(1,95)$ statistic is 0.83 , with a $p$-value of 0.3634 .
(2d) $\widehat{\alpha}=\frac{\widehat{\beta}_{1}}{1+\widehat{\beta}_{1}}=0.597$.
(3b-c) The OLS estimates of the parameters are as follows (s.e. in brackets):

| Specification | $\widehat{\beta}_{0}$ | $\widehat{\beta}_{1}$ | $\widehat{\beta}_{2}$ | $\widehat{\beta}_{3}$ | $\widehat{\sigma}^{2}$ | $R^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $H K(O L S)$ | 3.830 | 0.6967 | -1.745 | 0.654 | 0.257 | 0.7856 |
|  | $(1.180)$ | $(0.132)$ | $(0.4159)$ | $(0.0727)$ |  |  |
| $H K(R L S)$ | 6.514 | 0.8351 |  | 0.635 | 0.269 | 0.7738 |
|  | $(0.099)$ | $(0.120)$ |  | $(0.073)$ |  |  |

Table 3: OLS Estimates - Part 3
$(3 \mathrm{~d}) \widehat{\alpha}=\frac{\widehat{\beta}_{1}}{1+\widehat{\beta}_{1}}=0.455 ; \widehat{\gamma}=\widehat{\beta}_{3}(1-\widehat{\alpha})=0.288$.
(4a) The OLS estimates of the parameters are as follows (s.e. in brackets):

| Specification | $\widehat{\beta}_{0}$ | $\widehat{\beta}_{1}$ | $\widehat{\beta}_{2}$ | $\widehat{\sigma}^{2}$ | $R^{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $H K(O L S)$ | 6.937 | 0.993 | 0.348 | 0.463 | 0.6104 |
|  | $(0.124)$ | $(0.303)$ | $(0.195)$ |  |  |

Table 4: OLS Estimates - Part 4
$\widehat{\alpha}=\frac{\widehat{\beta}_{1}}{1+\widehat{\beta}_{1}}=0.498$, which implies that $\widehat{\rho}=0.3517$ and $\widehat{\sigma}=1.542$. We reject the C-D specification at the $8 \%$ level, because $\hat{\rho} \neq 0$, and there is evidence that the production function has an elasticity of substitution which is higher than the Cobb-Douglas case.

