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## Checklist for ECON 351\* Mid-Term Exam, Winter Term 2009

**Coverage of exam**    **Part I: Sections 1-5 on Course Outline; NOTES 1-9.**

### **Format of questions**

**Part 1: Definitions, Proofs, and Derivations**

**Part 2: Short Answer Questions (some requiring numerical answers)**

**Proofs and Derivations to Know** for regression model  $Y_i = \beta_0 + \beta_1 X_i + u_i$

- Derivation of OLS normal equations, the first-order conditions for the OLS coefficient estimators  $\hat{\beta}_0$  and  $\hat{\beta}_1$  from the RSS function
- Solution of OLS normal equations to obtain formulas for the OLS coefficient estimators  $\hat{\beta}_0$  and  $\hat{\beta}_1$
- Proof of linearity and unbiasedness of  $\hat{\beta}_1$ , i.e., proof that  $E(\hat{\beta}_1) = \beta_1$
- Derivation of expression (formula) for  $\text{Var}(\hat{\beta}_1)$
- Derivation of OLS decomposition equation from OLS SRE  $Y_i = \hat{Y}_i + \hat{u}_i$
- Derivations of the t-statistic for  $\hat{\beta}_1$  and the F-statistic for  $\hat{\beta}_1$
- Derivation of two-sided  $100(1-\alpha)$  percent confidence interval for  $\beta_1$  or  $\beta_0$
- Basic concepts of hypothesis testing

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**Important Things to Know** about regression model  $Y_i = \beta_0 + \beta_1 X_i + u_i$ 

- ◆ Assumptions A1-A8 of the Classical Linear Regression Model.
- ◆ Definition and meaning of the following statistical properties of estimators:  
(1) unbiasedness; (2) minimum variance; (3) efficiency.
- ◆ Statistical properties of the OLS coefficient estimators  $\hat{\beta}_0$  and  $\hat{\beta}_1$ .
- ◆ Computational properties of the OLS sample regression equation.
- ◆ How to compute and interpret OLS coefficient estimates  $\hat{\beta}_0$  and  $\hat{\beta}_1$ .
- ◆ How to compute estimated variances and standard errors of the OLS coefficient estimates  $\hat{\beta}_0$  and  $\hat{\beta}_1$ .
- ◆ How to compute and interpret the coefficient of determination  $R^2$ .
- ◆ The error normality assumption A9 and its implications for (1) the distribution of the  $Y_i$  values and (2) the sampling distributions of  $\hat{\beta}_0$  and  $\hat{\beta}_1$ .
- ◆ How to construct and interpret *two-sided* confidence intervals for  $\beta_0$  and  $\beta_1$ .
- ◆ How to perform *two-tail* and *one-tail* hypothesis tests for  $\beta_0$  and  $\beta_1$ .